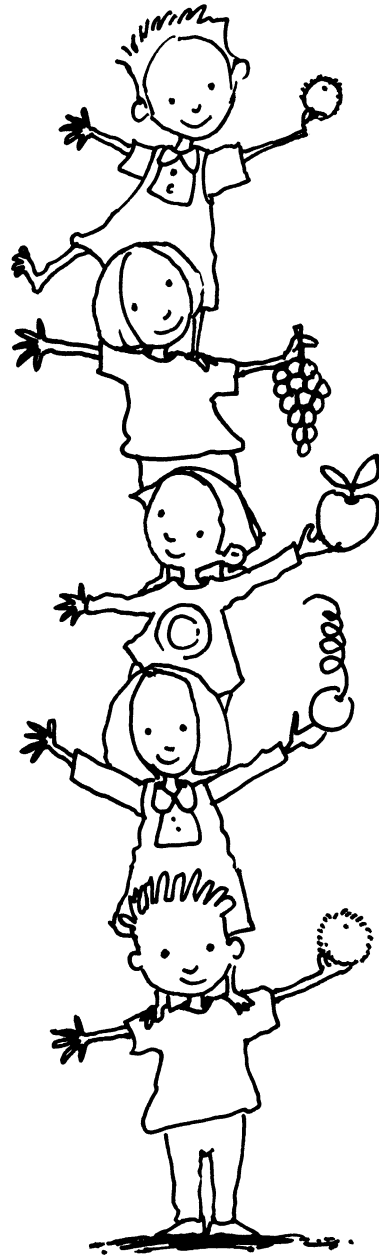


SOLVE
THAT PROBLEM!

Using Logical Reasoning



SOLVE
THAT PROBLEM!

SOLVE
THAT PROBLEM!

SOLVE
THAT PROBLEM!

Teaching Notes Using Logical Reasoning



Logical reasoning is unlike the 'guess and check' strategy, where random guesses are made. When logical reasoning is used, the problem solver begins with the knowledge that each piece of information is a piece of the puzzle, and that by putting the pieces together, they will be working towards a solution. The problem is then tackled step by step.

Pupils can approach these problems in different ways, working by a process of elimination, or using each piece of information to build towards the solution.

READ EACH CLUE THOROUGHLY

Reading each clue thoroughly is one of the vital skills in solving problems using logical reasoning. It is very important that pupils take the time to read the clues and understand each one. They can then decide where to begin in solving the problem.

DECIDE WHERE TO BEGIN

Often the clues need to be dealt with in a different order to the order in which they are presented.

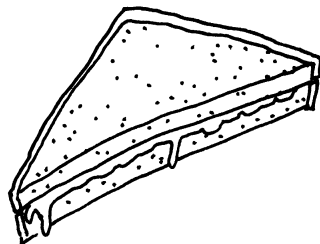
Example

Julie, Josh and Sam are each about to eat a sandwich for lunch. On the plate there is a tomato sandwich, a honey sandwich and a peanut butter sandwich. Use the following clues to work out which sandwich belongs to each person.

- Julie's sandwich has salt and pepper on it.
- Sam is allergic to nuts.
- Josh hates sweet things.

It is probably easiest to begin with the fact that Sam is allergic to nuts, which means the peanut butter sandwich cannot be his. Julie's sandwich has salt and pepper on it, so it is not likely to be the peanut butter sandwich. She must have the tomato sandwich. This leaves Sam with the honey sandwich (which Josh would not have had, since she hates sweet things).

So Julie has the tomato sandwich, Sam has the honey sandwich, and Josh has the peanut butter sandwich.



DRAW UP A GRID LISTING THE NAMES AND CHOICES

Drawing up a grid can be a convenient way of visualising the information presented in a problem, and clarifying the steps taken to solve it.

For the previous example, the grid would look like this:

	tomato	honey	peanut butter
Julie			
Josh			
Sam			

Once drawn up, a grid can be systematically marked up with ticks and crosses (or true and false, or yes and no, or whatever is most suitable) to clarify each step and visualise the information that has been given.

	tomato	honey	peanut butter
Julie	✓	✗	✗
Josh	✗	✗	✓
Sam	✗	✓	✗



Teaching Examples Using Logical Reasoning



EXAMPLE 1

Four children, Alan, Bernard, Tammi and Sue, own four dogs called Tom, Bubby, Susie and Arty. Use the information below to work out which dog belongs to which owner.

- Nobody owns a dog whose name starts with the same letter as their own.
- Tammi and Bubby's owner are friends.
- Bernard's sister owns Arty.
- Alan gives Susie's owner a bone.
- Susie's owner said Tammi's dog was aggressive.
- Alan wished he had a dog like Tom.

Understanding the problem

WHAT DO WE KNOW?

There are four children and they each owned a dog.

Each dog's name starts with a different letter to their owner's name.

WHAT DO WE NEED TO FIND OUT?

Questioning: Which dog belongs to which person?
Which clue will be a good starting point?

Communicating a solution

Draw up a 5 x 5 grid. Use the symbols ✓ and ✗ to represent the different pieces of information contained in the clues. For example, since we know that none of the owners' names begin with the same letter as their dogs' name, we can immediately put crosses in the boxes that link Alan and Arty, Bernard and Bubby, Tammi and Tom, and Sue and Susie.

Filling in the other pieces of information gives us this grid:

	Tom	Bubby	Susie	Arty
Alan	✗	✓	✗	✗
Bernard	✗	✗	✓	✗
Tammi	✗	✗	✗	✓
Sue	✓	✗	✗	✗

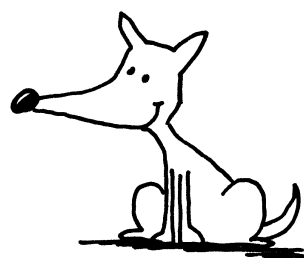
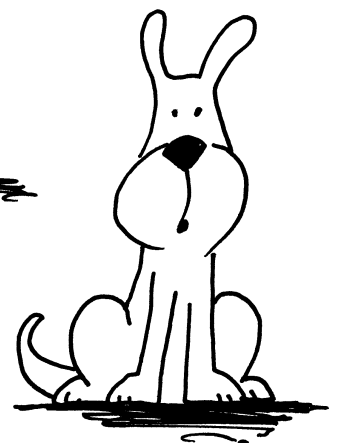
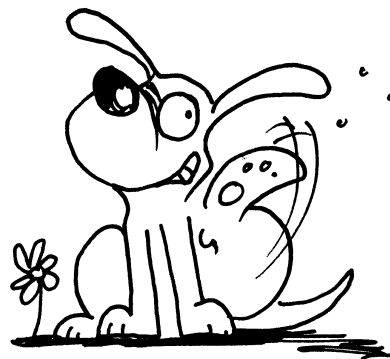
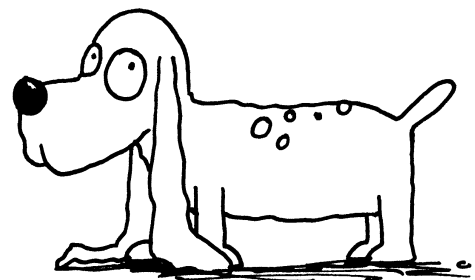
From this we can see that Alan owns Bubby, Bernard owns Susie, Tammi owns Arty and Sue owns Tom.

Reflecting and generalising

Think about the strategy of creating a grid and using ticks and crosses to represent the information provided. Is this a logical approach to use when a number of statements are made? Is there another way to solve this problem?

Extension

Encourage pupils to write simple problems of their own that include a number of logical statements and can be approached using this technique.



Teaching Examples Using Logical Reasoning



EXAMPLE 2

Twenty-four boarders live at a school where the rest of the pupils are day pupils. The boarding school is built in the shape of a square, divided into nine rooms. The pupils sleep three to a room, and the teacher sleeps in a room in the middle in order to supervise the pupils. At night the teacher has to ensure that there are nine pupils on each side of the square.

One night some of the boarders slipped out. How did the pupils manage to deceive their teacher? What is the greatest number of pupils that could go out at a time and still leave nine pupils on each side of the square?

Understanding the problem

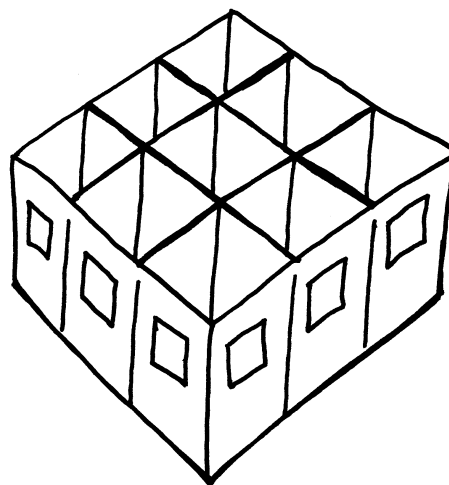
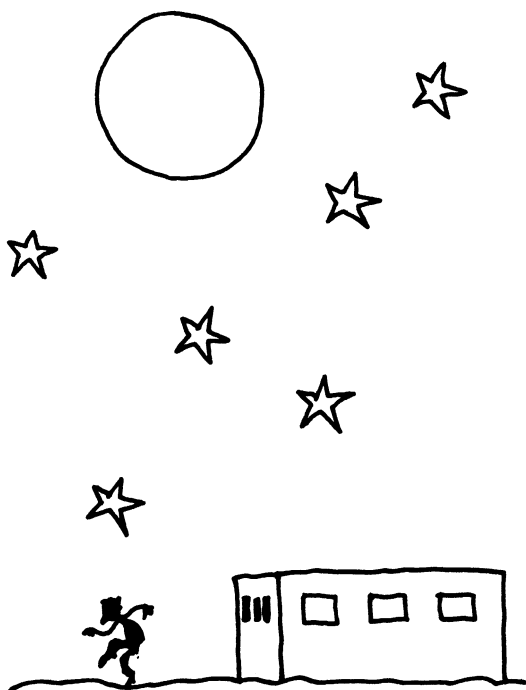
WHAT DO WE KNOW?

There are 24 boarders. Pupils sleep three to a room. The teacher sleeps in the middle room. The boarding school is built in the shape of a square. There have to be 9 pupils on each side.

WHAT DO WE NEED TO FIND OUT?

Questioning: How did they manage to deceive the teacher?

What is the greatest number of pupils that could go out at a time and still do this?



Communicating a solution

The corner rooms are counted in both directions, so more pupils should be placed in those rooms.

5	1	3
1		1
3	1	5

In this way, 4 pupils could sneak out and still leave nine pupils on each side.

Six is the greatest number that can go out as 18 pupils must be left inside.

9	0	0
0		0
0	0	9

Reflecting and generalising

The first logical step utilises the knowledge that the corner pupils are counted twice. To allow more pupils to sneak out, more of the pupils that remain should therefore be placed in the corner rooms. This concept should be applied to other problems where there are limited numbers that can be used for maximum advantage.

Extension

Ask pupils to calculate the problem changing the number of pupils that are boarders and the number that need to stay at home. Are they able to apply the same concepts to different numbers?

Teaching Examples Using Logical Reasoning



EXAMPLE 3

Five children, Andy, Jocelyn, Nick, Rob and Kahlee, brought their favourite fruits to school. They brought peaches, apples, grapes, apricots and passionfruit. Use the clues below to work out which person brought which fruit.

- Jocelyn's favourite fruit is passionfruit. Andy's favourite fruit starts with the same letter.
- Nick's and Rob's fruit don't start with the same letter.
- Nick likes apples.

Understanding the problem

WHAT DO WE KNOW?

Five children brought their favourite fruit to school. They brought peaches, apples, grapes, apricots and passionfruit.

WHAT DO WE NEED TO FIND OUT?

Questioning: What fruit did each person bring?

Communicating a solution

Draw up a grid that is 6 x 6. Write the names of the children down the left hand side of the grid and the names of the fruit along the top of the grid.

	peaches	apples	passionfruit	grapes	apricots
Andy	✓	✗	✗	✗	✗
Jocelyn	✗	✗	✓	✗	✗
Nick	✗	✓	✗	✗	✗
Rob	✗	✗	✗	✓	✗
Kahlee	✗	✗	✗	✗	✓

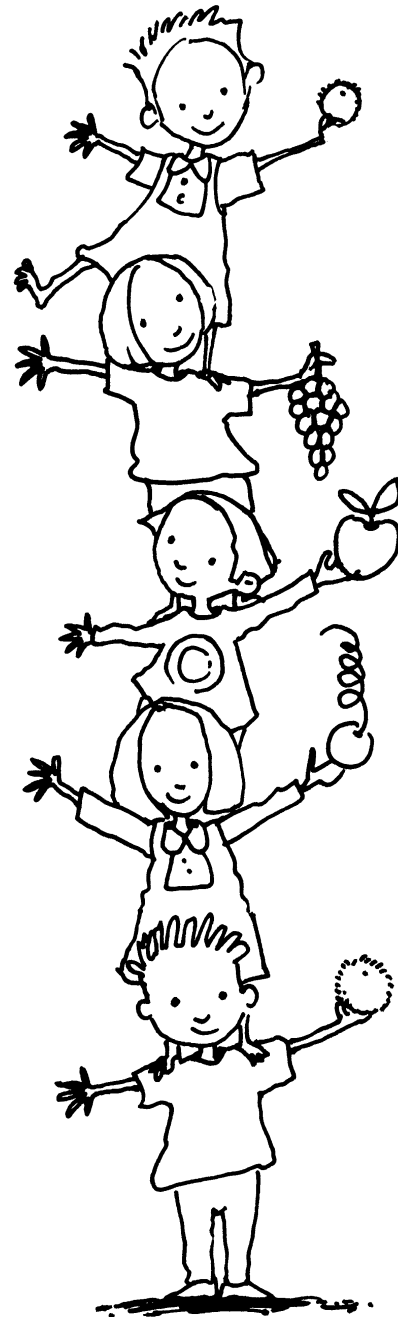
Andy brought the peaches, Jocelyn brought the passionfruit, Nick had the apples, Rob had the grapes, and Kahlee had the apricots.

Reflecting and generalising

The information was checked off using a system of ticks and crosses that helped with the visualisation and allowed us to put the clues into a concrete form.

Extension

Ask pupils to prepare a logical problem using six people and six objects. They will need to ensure that they have included enough clues to allow the problem to be solved.



Copymaster Using Logical Reasoning



★ Understanding the problem

List the facts that will be important in finding the solution:.....

.....

★ What do you need to find out?

What questions do you have? What are you uncertain about? Is there any unfamiliar or unclear language?.....

.....

★ Planning and communicating a solution

Will you work logically? In what order will you use the clues? Will you find one that can be used as a starting point and from which the others can be logically thought out? Will you use a grid to help visualise the clues? Will you use objects to stand for the people and places in order to help visualise the situation?.....

.....

.....

.....

★ Reflecting and generalising

Did the strategy work as planned? Will you be able to apply this method of problem solving to other similar problems? Would a different method have worked better for you for this problem?.....

.....

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★ Extension

How can this strategy be applied to more complicated problems involving additional factors?.....

.....

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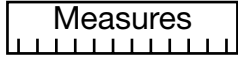
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PROBLEM SOLVING TASK CARDS

Using Logical Reasoning

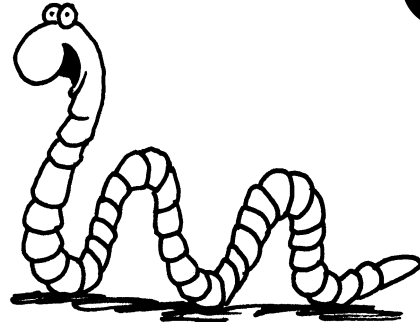
Problem 91

Measures



Level
A

In the story Harry was reading, a forever-hungry worm ate everything in sight. It ate so much that, incredibly, it doubled its size every day. If it took 11 days for the worm to be fully grown, how long did it take the worm to get to half its full-grown size?



Problem 92

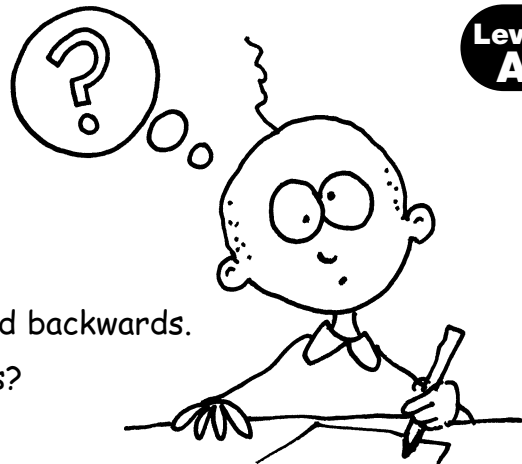
Numbers 123

Level
A

There are three different numbers.

- They are all four-digit odd numbers.
- The digits of each number add up to 14.
- None of the numbers can be divided by 5.
- These numbers read the same forwards and backwards.

Can you guess the numbers using these clues?

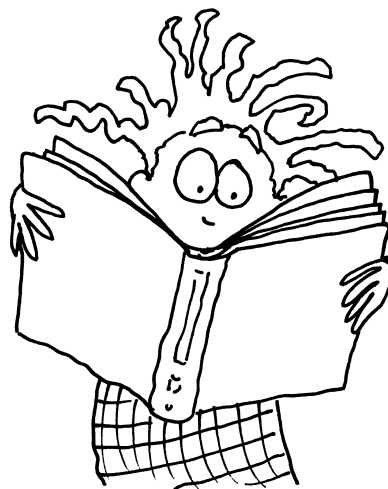


Problem 93

Numbers 123

Level
A

When Clarice opened her book, she saw two numbered pages. The sum of these two pages was 317. What would the next page number be?



PROBLEM SOLVING TASK CARDS

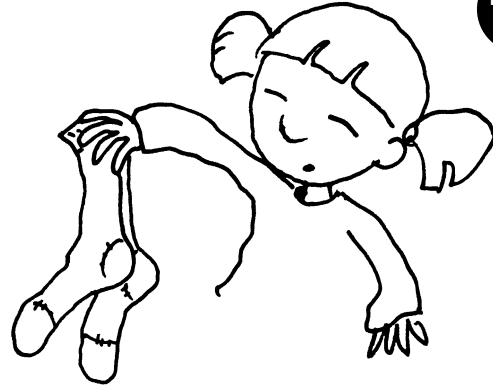
Using Logical Reasoning

Problem 94

Numbers **123**

Level **A**

I have 30 socks in my drawer and they vary in colour. I have 12 black, 10 blue, 2 brown and 6 grey socks. If I close my eyes and pull socks out at random, how many socks must I pull out before I can be certain to have a matching pair?

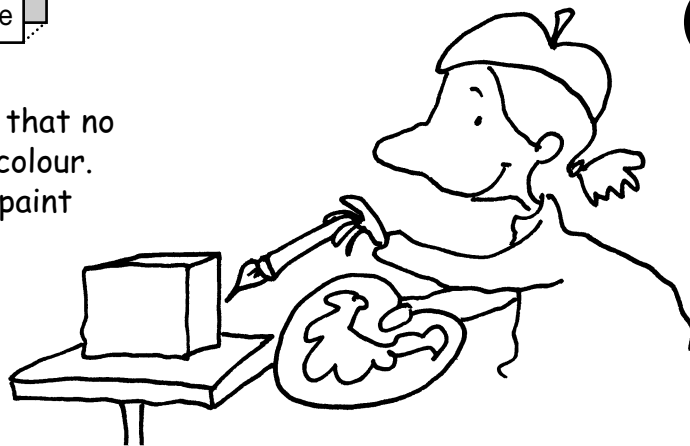


Problem 95

Shape & Space

Level **A**

Rani wants to paint a cube so that no opposite faces are the same colour. What is the least number of paint colours she should buy?

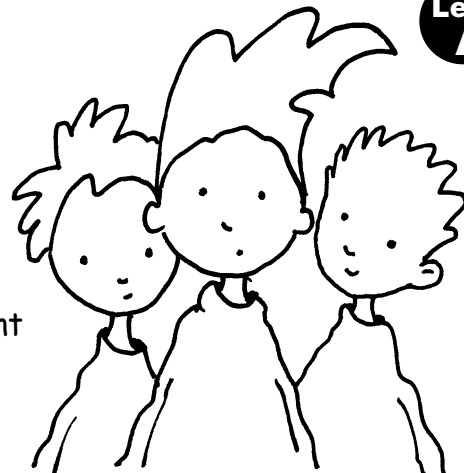


Problem 96

Numbers **123**

Level **A**

When Tristram, Evelyn and Carol leave school, they want to work in one of the following professions: as a teacher, an engineer or a computer programmer. None of them wants to work in a profession starting with the same letter as their name. Evelyn's mother is the aunt of the person who wants to become a teacher. What does each person want to become?



PROBLEM SOLVING TASK CARDS

Using Logical Reasoning

Problem 97

Measures

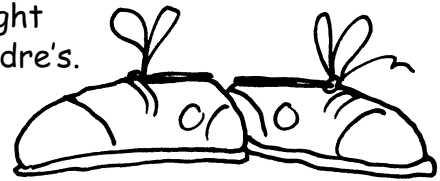
Level
B

Five pupils left their shoes in the changing rooms. Each wore the same brand of shoes, but in a different size. The shoes were sizes 2, 3, 4, 5 and 6.

Tensu knew that his were the smallest. Karen thought hers were bigger than Chan's but smaller than Deirdre's.

Brad knew his were the largest.

Which size shoes did each pupil have?



Problem 98

Numbers 123

Level
B

There are 105 animals living on Farrelly's Farm. There are half as many rabbits as guinea pigs. There are half as many geese as sheep. There are three times as many geese as guinea pigs. How many of each farm animal are there?



Problem 99

Measures

Level
B



The pupils at camp hold a running race. Use these clues to work out their positions at the end of the race.

Peter was extremely fast and was the first boy to complete the race. Lisa came in just before Jonathan. Jonathan finished after Catherine. Michelle ran very well and managed to beat Catherine. Peter finished after Michelle but before Catherine.

PROBLEM SOLVING TASK CARDS

Using Logical Reasoning

Problem 100

Shape & Space

Level
B

Thomas and Trina help their parents with the chores at home. Complete a grid to show the order in which each completes their chores.

- Thomas vacuums the carpet after Trina dries the dishes.
- The person who cleans the bathroom does this first.
- The dishwasher is emptied before the mail is collected. Different people do these tasks.
- The last thing that Trina does is take the dog for a walk.
- Trina does not walk the dog at the same time as the carpet is being vacuumed.

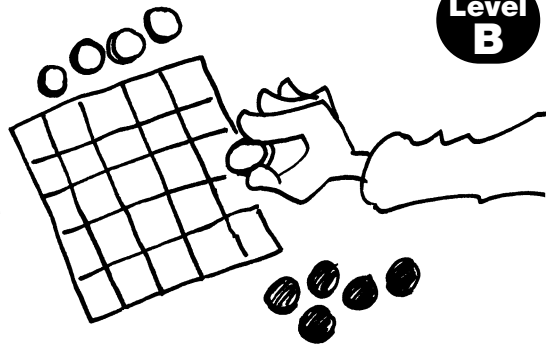


Problem 101

Numbers 123

Level
B

Draw up a five by five square chart. You will need five sets of coloured counters, with five of each colour. Place the coloured counters on the chart so that there is one of each colour in each row, column and diagonal.



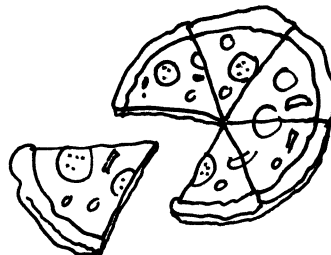
Problem 102

Numbers 123

Level
B

Carter, Jackie, Despina and Fred ordered pizza slices. They could choose from peperoni, vegetarian, anchovies and cheese. Match each person with the pizza they ordered.

- Carter hates all seafood.
- Jackie can't eat milk products.
- Despina loves meat.
- Fred is a vegetarian.



PROBLEM SOLVING TASK CARDS

Using Logical Reasoning

Problem 103

Numbers **123**

Level
C

Carmen bought five tickets to watch a game of football with her friends. The tickets were numbered in order. When the numbers are added together, they total 110. What were the ticket numbers.



Problem 104

Numbers **123**

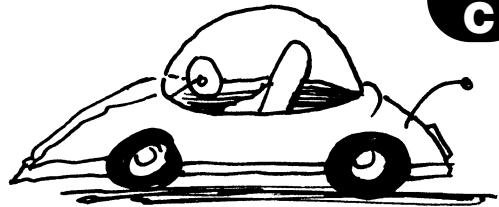
Level
C

Five cars are in a race. Their numberplates are:

1733 5824 9762 6465 7525

- The car with the highest number finished last.
- When the digits in the numberplates of the cars that came first and second are added, they give the same total.
- The cars that came in third and fourth both have an odd number as the last digit.
- The cars that came in second and third both bear numbers that are multiples of five.

Use these clues to work out how the racing cars placed in the race.



Problem 105

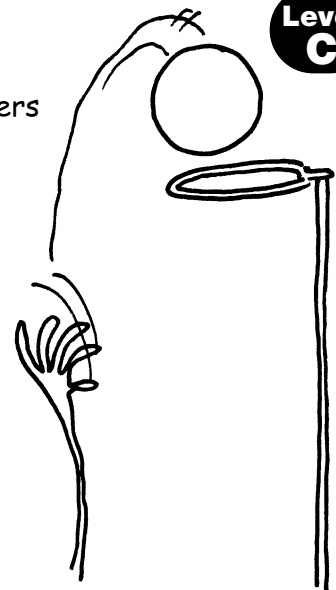
Numbers **123**

Level
C

Jennifer, Jackie, Tandi, Lindsay, Sara and Lesley are all shooters in different netball teams. Between them one Saturday they scored a total of 33 goals. Each girl scored a different number of goals and each girl scored at least one goal.

- Jennifer was the top scorer and scored three more than Jackie.
- Tandi scored one less than Lindsay but their total was the same as Jennifer's and Jackie's scores added together.
- Lesley beat Sara's scoring level but their scores together equalled the number of goals Lindsay had scored on her own.

Use these clues to work out how many goals each girl scored.



PROBLEM SOLVING TASK CARDS

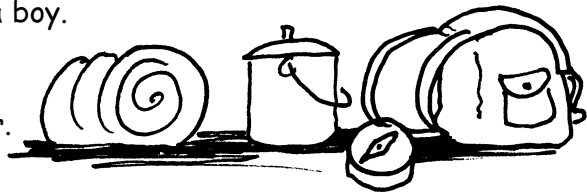
Using Logical Reasoning

Problem 106 Numbers 123

Level C

Jane, Graham, Rebecca and Paul are planning their camping holiday this year. Each wants to visit a different place. One wants to go to Painton, another to Gosport, the third to Margate and the last to Great Yarmouth. Use the clues to work out who wants to go where.

- No-one wants to visit the place starting with the same letter as their name.
- The person who wants to visit Margate is a boy.
- A boy wants to visit Gosport.
- Graham likes Margate and Gosport.
- Jane did not want to visit Painton this year.

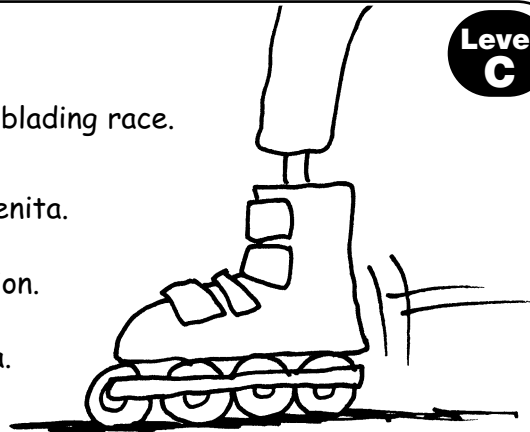


Problem 107 Shape & Space

Level C

Dirk, Arthur, Benita, Caren and Edie had a roller-blading race. Use the clues to work out their finishing order.

- Caren did not finish just before or just after Benita.
- Dirk finished just in front of Benita.
- Neither Arthur nor Benita finished in last position.
- Caren wasn't in first or last place.
- Dirk completed the route just in front of Benita.
- Edie didn't finish just before or after Caren.



Problem 108 Shape & Space

Level C

Four friends—Rudi, Maya, Jeff and Frances—went out for lunch. When they sat down at the table, each was wearing a different coloured shirt. Their shirts were black, yellow, white and blue. Each ordered something different for lunch: a hamburger, a pizza slice, a hot dog and a sandwich. Work out who sat in which seat, which colour shirt they were wearing and what each ordered to eat.

The friend in black sat opposite the friend in white who ordered the slice of pizza. The friend in yellow was not sitting in a westerly or southerly seat. Jeff sat in the northerly seat. The person who sat opposite Jeff had a hamburger to eat. The person in the easterly seat had a hot dog and wore a black shirt. This wasn't Frances, who was wearing a blue shirt. Maya sat in the westerly seat.

Answers to Task Cards

Using Logical Reasoning

Problem 91

10 days. As it doubles its size every day and is fully grown by day 11, it would be half its full-grown size on day 10.

Problem 92

The numbers are 1661, 3443 and 7007.

Problem 93

The next page number is 160. Clarice knows that one of the pages must be one higher than the other page number. Dividing 317 by two gives 158 with one remaining. So the page numbers she can see must be 158 and 159.

Problem 94

I would need to pull out 5 socks. Because there are four different colours, even if I pull out a different coloured sock each time on the first four goes, the fifth has to provide a matching sock.

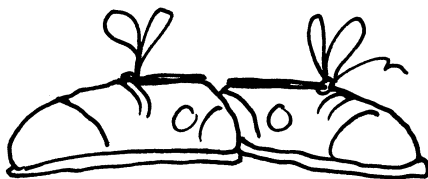
Problem 95

Two colours. Supply pupils with the net of a cube so that they can experiment with colours. Point out that the problem states opposite faces cannot be the same colour, but that this does not apply to adjacent faces.

Problem 96

	Teacher	Engineer	Computer programmer
Tristram	✓	✗	✗
Evelyn	✗	✓	✗
Carol	✗	✗	✓

(Because you are told that Evelyn's mother is the aunt of the person who wants to be the teacher, you know that Evelyn herself does not want to be a teacher.)



Problem 97

	2	3	4	5	6
Tensu	✓	✗	✗	✗	✗
Karen	✗	✗	✓	✗	✗
Chan	✗	✓	✗	✗	✗
Deirdre	✗	✗	✗	✓	✗
Brad	✗	✗	✗	✗	✓

So Tensu wears size 2, Chan size 3, Karen size 4, Deirdre size 5 and Brad size 6.

Problem 98

5 rabbits, 10 guinea pigs, 30 geese, 60 sheep. Have pupils start by putting the animals in order from least to most.

Problem 99

	1st	2nd	3rd	4th	5th
Peter	✗	✓	✗	✗	✗
Lisa	✗	✗	✗	✓	✗
Jonathan	✗	✗	✗	✗	✓
Catherine	✗	✗	✓	✗	✗
Michelle	✓	✗	✗	✗	✗

Problem 100

Thomas	Trina
cleans the bathroom	dries the dishes
vacuums the carpet	empties the dishwasher
collects the mail	walks the dog

Problem 101

There are several solutions. One of them is:

R	B	G	W	Y
W	Y	R	B	G
B	G	W	Y	R
Y	R	B	G	W
G	W	Y	R	B

R = red
 B = blue
 G = green
 Y = yellow
 W = white

Answers to Task Cards

Using Logical Reasoning

Problem 102

	peperoni	vegetarian	anchovies	cheese
Carter	x	x	x	✓
Jackie	x	x	✓	x
Despina	✓	x	x	x
Fred	x	✓	x	x

Problem 103

The ticket numbers are 20, 21, 22, 23, 24. The average number for each ticket is 22 ($110 \div 5$). Work forwards and backwards from 22.

Problem 104

First	5824
Second	7525
Third	6465
Fourth	1733
Fifth	9762

Problem 105

Jennifer	8 goals
Lindsay	7 goals
Tandi	6 goals
Jackie	5 goals
Lisa	4 goals
Sara	3 goals

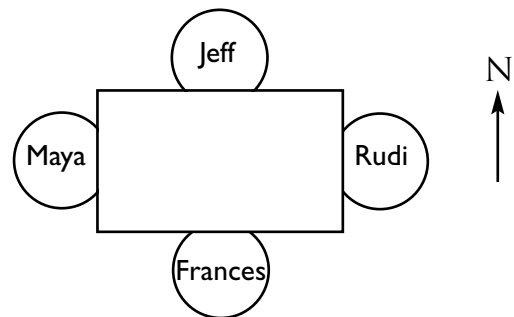
Problem 106

	Painton	Gosport	Margate	Great Yarmouth
Jane	x	x	x	✓
Graham	x	x	✓	x
Rebecca	✓	x	x	x
Paul	x	✓	x	x

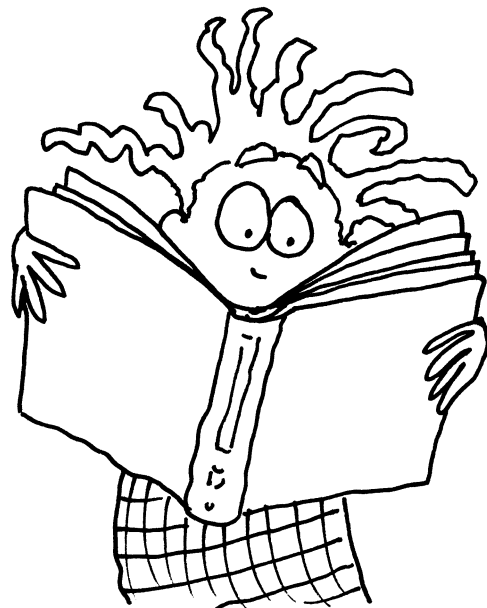
Problem 107

	1st	2nd	3rd	4th	5th
Dick	x	x	✓	x	x
Arthur	✓	x	x	x	x
Benita	x	x	x	✓	x
Caren	x	✓	x	x	x
Edie	x	x	x	x	✓

Problem 108



Rudi, black shirt, hot dog
 Maya, white shirt, pizza
 Jeff, yellow shirt, sandwich
 Frances, blue shirt, hamburger



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